

Engineering Physics

Physics for Forestry

Electricity

Electrostatics

- Electrostatics deals with the interaction of electric charges at rest and the electric fields associated with them
- Each atom consists of a positively charged nucleus containing protons and neutrons, surrounded by negatively charged electrons (neutrons are neutral)
- In an electrically neutral atom, there are just as many electrons (e^-) outside the nucleus as there are protons in the nucleus (e^+)
- The smallest charge (charge of electron or proton): the elementary charge $e = 1.6 \cdot 10^{-19}$ C (SI unit of charge is coulomb – C)
- Every electric charge is quantized - all charges are integer multiples of the elementary charge

Electrostatics

- Ion - an atom that has either lost one or more electrons, making it positively charged (+ Q), or gained one or more electrons, making it negatively charged (- Q)

Coulomb's Law

The magnitude of force between two point charges is directly proportional to the product of charges Q and Q_0 , and is inversely proportional to the square of the distance d between them: $F_e = \frac{1}{4\pi\epsilon} \cdot \frac{QQ_0}{d^2}$, where

ϵ – permittivity of medium: $\epsilon = \epsilon_0\epsilon_r$

$\epsilon_0 = 8.854 \cdot 10^{-12}$ F/m – the permittivity of vacuum

ϵ_r – relative permittivity

Electrostatics

- Between any charges acts force:
- consonant charges repel each other - *repulsive force*
- discordant charges attract each other - *attractive force*

Electric field

- There is a space around the charge in which a force field - an electric field - can be detected
- The electric field around a charge at rest – the electrostatic field
- A force is exerted on a charged object placed in an electric field

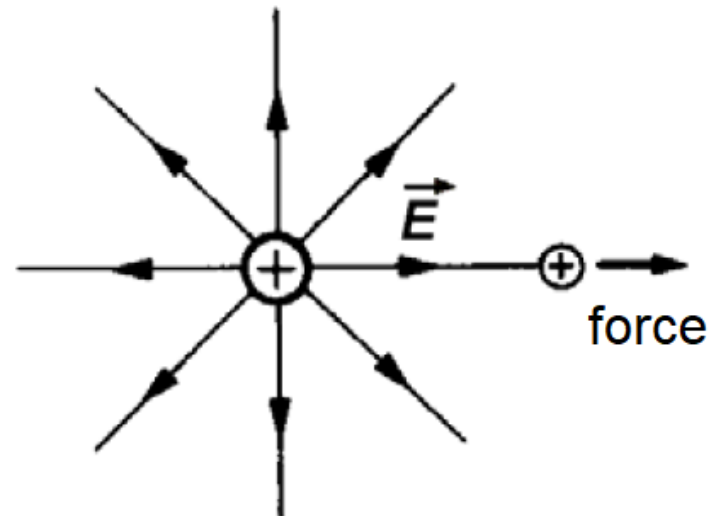
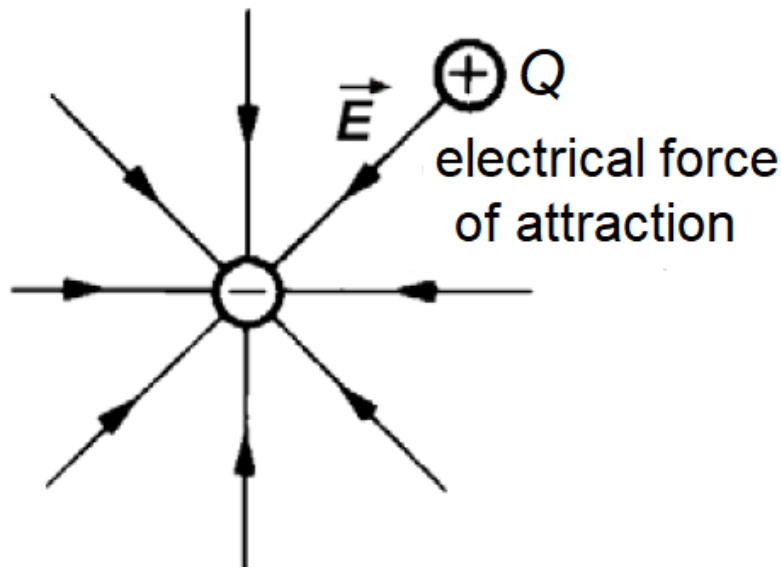
The intensity of electric field \vec{E} around charge Q at any point at distance d :

$\vec{E} = \frac{\vec{F}}{Q_0}$ – the force \vec{F} acting on the unit positive charge (1C)

- SI unit of intensity of electric field $[E] = \text{N/C}$ or V/m (volt per metre)

Electrostatics

- From Coulomb's law, the magnitude of the intensity of electric field E around a point charge Q at distance d : $E = \frac{1}{4\pi\epsilon} \cdot \frac{Q}{d^2}$
- The intensity of electric field \vec{E} – a vector quantity, the direction of this vector at any point is the direction of the force that would act on a positive charge located at that point – see Fig.



Electrostatics

Electric potential

- The *electric potential* V_A at point A is defined as the work done by the electric field in moving a unit positive charge from this point to infinity:

$$V_A = \frac{W_{A\infty}}{Q} = \int_A^\infty \frac{\vec{F} \cdot d\vec{r}}{Q} = \int_A^\infty \frac{\vec{E} \cdot Q}{Q} \cdot d\vec{r} = \int_A^\infty \vec{E} \cdot d\vec{r}$$

- The electric potential of a point charge at a distance d : $V(d) = \frac{1}{4\pi\epsilon} \cdot \frac{Q}{d}$
- Electric potential: a scalar quantity, positive for positive charge and negative for negative charge

Voltage: difference in electric potentials between two points:

$$U_{AB} = V_A - V_B$$

- Unit of electric potential and potential difference – volt $[V] = [U] = \text{J/C} = \text{V}$

Electrostatics

Conductors and insulators

- *Insulators or non-conductors*: materials such as glass, rubber, porcelain, etc. – do not allow the free passage of charge
- *Conductors*: metals, carbon and some liquids – charge can flow through them
- The best conductors: copper, silver and gold
- There is also a category "between" conductors and non-conductors: *semiconductors*

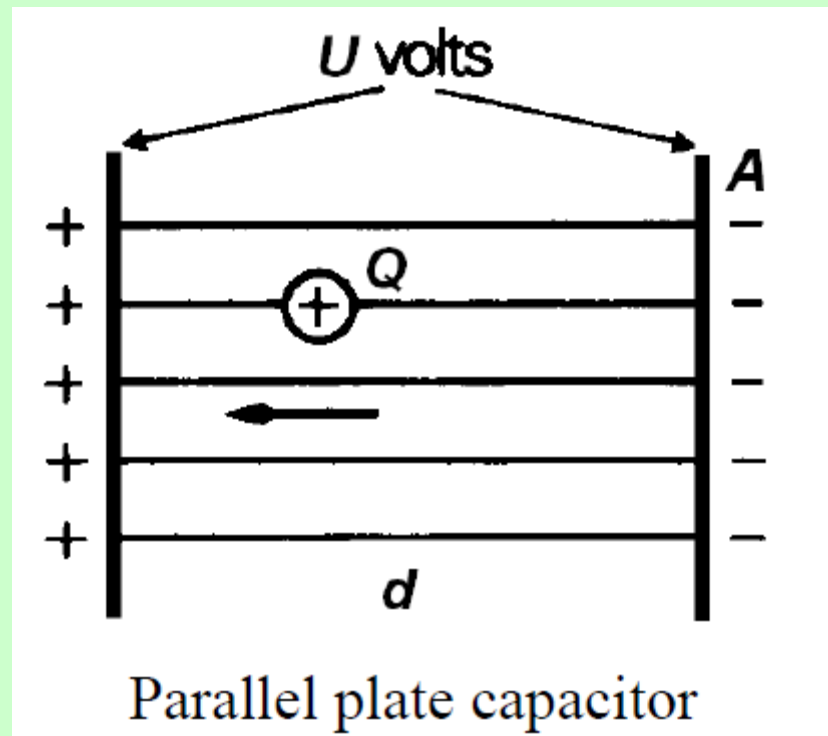
Electrostatics

Capacitance and capacitors

- If a charge is given to a conductor, the electric potential of the conductor is raised
- The *capacitance* C of a conductor for storing charge: the ratio of its charge Q to the potential difference U between two conductors or between a conductor and ground: $C = Q / U$
- SI unit of capacitance: $[C] = C/V = F$ (farad)
- A capacitor – the device for storing charge
- The simplest example of a capacitor: parallel plate capacitor – see Fig.
- It consists of two metal plates of area A , distance d separating them
- The space between the plates is filled by dielectric (insulating material) of permittivity ϵ

Electrostatics

- The capacitance C of parallel plate capacitor: $C = \frac{\epsilon A}{d}$
- The capacitance – constant for a given capacitor
- The value of the capacitance depends on area of metal plates, on their relative position and on the material that separates them



Electrostatics

Application

- A charged capacitor stores electrical energy

The energy stored in the capacitor is equal to the work done in charging it

- The work required to add a small charge dQ from one plate to the other plate: $dW = U dQ$, where U is the potential difference across the plates

- Total work done: $W = \int_0^Q U dQ = \frac{1}{C} \int_0^Q Q dQ = \frac{1}{2} \frac{Q^2}{C}$

- Energy stored in capacitor: $E = \frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} C U^2 = \frac{1}{2} Q U$

- It gives for a parallel plate capacitor: $E = \frac{1}{2} C U^2 = \frac{1}{2} \left(\frac{\epsilon A}{d} \right) E^2 d^2 = \frac{1}{2} \epsilon A E^2 d$

- This storing a large amount of energy can be released during a very short time – for example flashlight of camera

Electrostatics

Example 8.4:

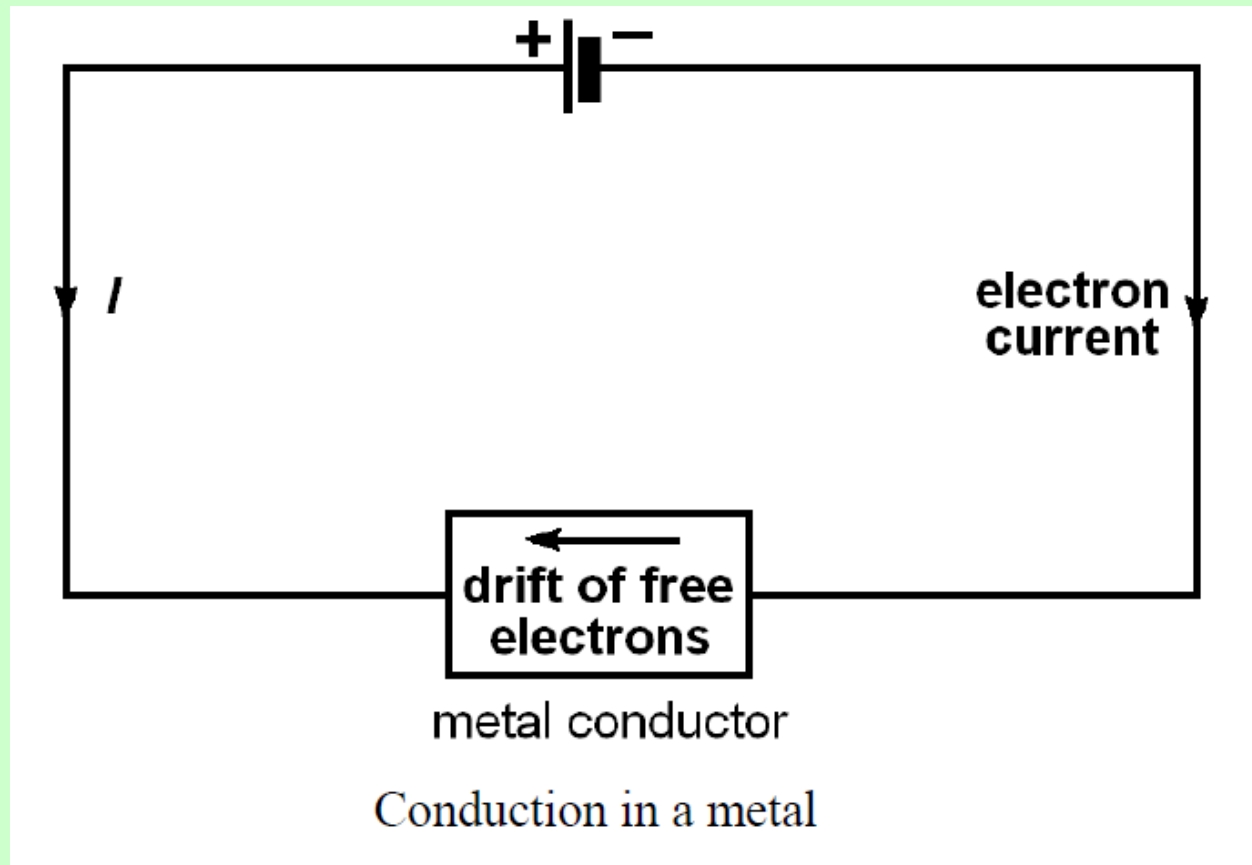
Two point electric charges act on each other in paraffin from a distance $d_1 = 2$ cm with a force of magnitude F . To act on each other in air with a force of the same magnitude F , they must be separated by $d_2 = 2.9$ cm. What is the relative permittivity of paraffin ϵ_{r1} ? The relative permittivity of air $\epsilon_{r2} = 1$.

$[\epsilon_{r1} = 2.1]$

Electric current

- Electric current – the ordered movement of electric charges
- An electric force is required to move the charge
- The force on the electrons in the conductor produces a current
- In a battery (potential difference source), one plate has a positive potential and the other plate has a negative potential
- The battery provides the *electromotive force* (e.m.f.) for electrons to flow through the metal conductor
- When the conductor is placed in a circuit containing the battery, the movement of free electrons is directed toward the positive plate
- The flow of electrons is directed from the negative to the positive plate
- The speed of the free electrons in random thermal motion becomes directional – *drift speed* – see Fig.

Electric current



- **Conventional electric current I** – the direction of positive charge in an electric field; from a point of positive (higher) potential to a point of negative (lower) potential

Electric current

- The electric current I – the amount of charge Q which passes through the cross-section of wire per unit of time t : $I = \frac{Q}{t}$
- Unit of current – coulomb per second – ampere, basic unit of SI system:
 $[I] = C/s = A$
- Current can flow in a circuit if there is a potential difference U - the terminals of the potential source (battery) are connected by conductors (metallic wire) and form an electrical circuit
- The electric current in the metallic conductor is proportional to the potential difference applied to its ends ($I \sim U$)
- The ratio of the potential difference to the current = constant
- The value of this constant – the *resistance* R of the conductor:
 $R = U / I$ or $U = R I$ – Ohm's law; the SI unit of resistance: ohm $[R] = \Omega$

Electric current

- The resistance R of a homogeneous isotropic metal wire is directly proportional to its length l and inversely proportional to the cross-

sectional area A of the wire: $R = \frac{\rho l}{A}$,

ρ – resistivity - the material constant of wire, $[\rho] = \Omega \cdot \text{m}$

- The resistance of materials depends on the temperature

- The resistance of conductors – directly proportional to the actual temperature: $\Delta R = R_0 \alpha \Delta t$, where

$\Delta R = R - R_0$, R – the resistance for final temperature t ,

R_0 – resistance for initial temperature t_0 ,

$\Delta t = t - t_0$ – change of temperature,

α – the temperature coefficient of resistance $[\alpha] = \text{K}^{-1}$

Electric current

Example 8.19:

Calculate the length of a constantan wire (60 % Cu, 40 % Ni) of diameter $d = 0.1$ mm if its resistance is to be $R = 1000 \Omega$. The resistivity of the constantan $\rho = 0.49 \mu\Omega \cdot \text{m}$.

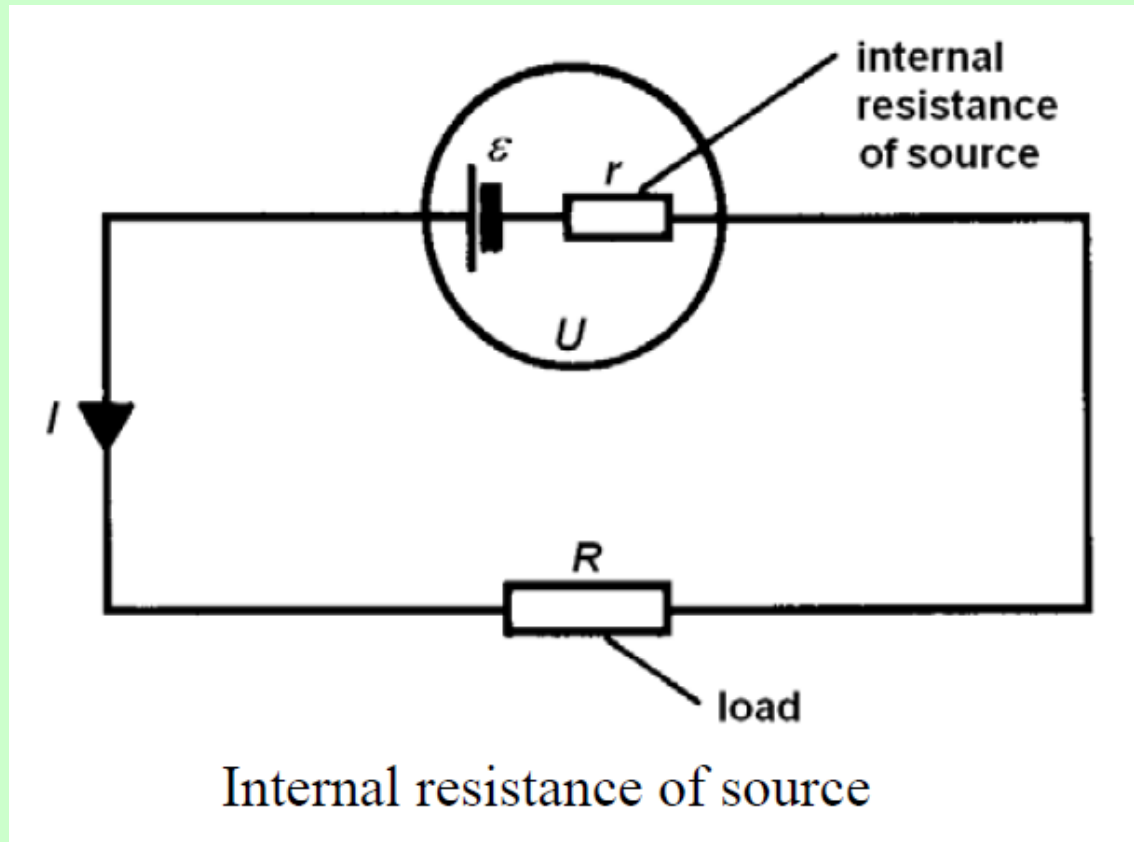
$[l = 16.03 \text{ m}]$

Electric current

Resistors

- All electric components in a circuit have a resistance
- The internal resistance r is inside the power source, for example a battery - see Fig.
- If the circuit is disconnected, no current flows through it \Rightarrow the electromotive force ε (e.m.f.) is across the terminals of the power supply
- If the circuit is connected, the source energizes the circuit, current I flows in the circuit, and the potential loss $I \cdot r$ is converted to heat inside the source \Rightarrow the potential difference (voltage) U across the source terminals is less: $U = \varepsilon - I \cdot r$

Electric current



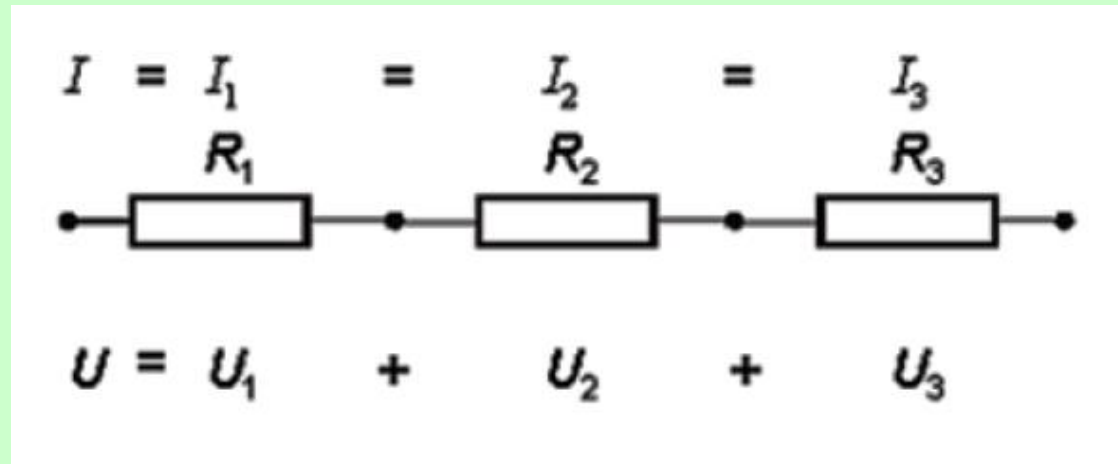
The current I which flows in a circuit is determined with a *total resistance* $R_{\text{total}} = R + r$ and with e.m.f. ε of the power supply:

$$I = \frac{\varepsilon}{R + r}$$

Electric current

Combination of resistors

Resistors connected in series – see Fig.



- The current I must be the same throughout the circuit because it has only one path
- If R is the total resistance of the combination of resistors and U is the total potential difference across them, then $U = I R$, the total potential difference U is the sum of the potential differences across resistors R_1 , R_2 , R_3

Electric current

- Thus:

$$U = U_1 + U_2 + U_3$$

$$\text{and } U = I R_1 + I R_2 + I R_3$$

$$\text{therefore } I R = I R_1 + I R_2 + I R_3$$

$$\text{and hence } R = R_1 + R_2 + R_3$$

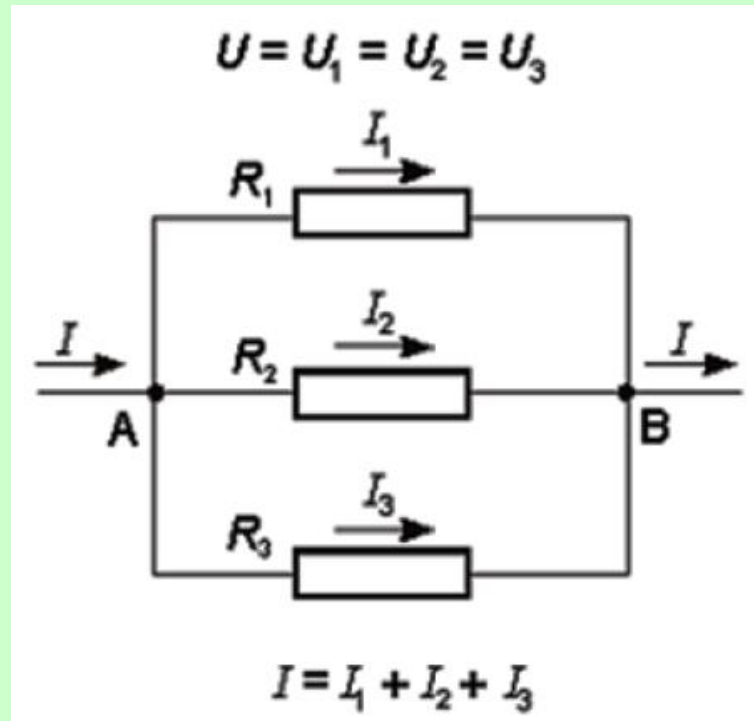
- The total resistance of the series connected resistors R is the sum of the individual resistances R_1, R_2, R_3

- The same result can be applied to n resistors in series:

$$R = \sum_{i=1}^n R_i$$

Electric current

Resistors connected in parallel – see Fig.



- The total current I in the main circuit is equal to the sum of the currents flowing in the parallel branches
- In a parallel circuit, the total current entering the junction must equal the total current leaving the junction

Electric current

- The potential difference U across all parallel resistors is the same
- If R is total resistance of the combination and I is the total current, then:

$$I = \frac{U}{R},$$

but I is the sum of the currents flowing in resistors R_1, R_2, R_3

Thus $I = I_1 + I_2 + I_3$, therefore $\frac{U}{R} = \frac{U}{R_1} + \frac{U}{R_2} + \frac{U}{R_3}$ and hence $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$

- The reciprocal value of the total resistance of the resistors connected in parallel is the sum of the reciprocal values of the individual resistors R_1, R_2, R_3
- The same result can be applied to n resistors in parallel:

$$\frac{1}{R} = \sum_{i=1}^n \frac{1}{R_i}$$

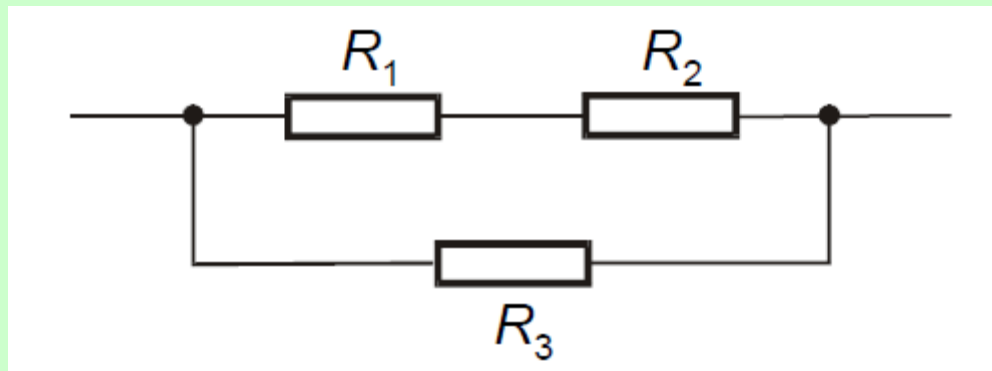
Electric current

Example 8.22:

Three resistors with resistances $R_1 = 100 \, \Omega$, $R_2 = 200 \, \Omega$ and $R_3 = 400 \, \Omega$ are connected according to the diagram.

Calculate their resulting resistance R .

[$R = 171 \, \Omega$]



Electric current

Electric energy

- From the definition of potential difference (voltage) and electric current it follows that if a potential difference U is applied to the ends of a conductor and a charge Q passes through it, then the work W done in time t : $W = U I t$

Application

- The work of an electric current - electrical energy - is converted into other forms of energy

- In an electric heater it is converted into heat $Q = U I t$, in an electric bulb into light and heat, in an electric motor into mechanical energy of rotation, etc.

Electric current

Electric power

- The definition of power P is the rate of work W done and time t taken
- Using the equations for electric energy and Ohm's law:

$$P = \frac{W}{t} = UI = RI^2 = \frac{U^2}{R}, [P] = \text{W (watt)}$$

Application

From the definition of power $P = \frac{W}{t} \Rightarrow W = P t \Rightarrow$

\Rightarrow unit of work (electric energy) $[W] = [P] \cdot [t] = \text{W} \cdot \text{s}$

- The commercial unit of electric energy – kilowatt-hour (kWh):

$$1 \text{ kWh} = 1000 \cdot 3600 \text{ W} \cdot \text{s (J)} = 3.6 \text{ MJ}$$

- Electricity is billed using the unit kilowatt-hour
- Total energy consumed (number of kWh) x price per unit = total electricity charge