# **Engineering Physics Physics for Forestry**

Magnetism

- There is an electric field in the space around the charge at rest
- There is a force acting on each charged object placed in this electric field
- The physical quantity that describes the electric field is the intensity of electric field  $\vec{E}$
- When a charge moves, it is the source of another field in its surroundings the magnetic field
- A force acts on a moving charged object placed in this magnetic field
- A magnetic field is described by the intensity of magnetic field  $\vec{H}$  or by the magnetic induction  $\vec{B}$
- These two quantities are related by  $\vec{B} = \mu \vec{H}$ , where  $\mu$  is the permeability of the medium

- SI units of these quantities:
- [*H*] = A/m, [*B*] = T (tesla) or Wb/m<sup>2</sup>
- $\mu = \mu_0 \ \mu_r$  , [ $\mu$ ]= H/m
- $\mu_0 = 4\pi \cdot 10^{-7}$  H/m permeability of vacuum
- $\mu_{\rm r}$  relative permeability of medium

- The magnetic field is represented by magnetic field lines, which show the direction of the force acting on the north pole of the permanent magnet at different points of this magnetic field - the direction of the vector  $\vec{B}$ 

- The north pole of the magnet attracts the south pole and repels the north pole
- The consonant poles of the magnets repel each other, the discordant poles attract each other

- When a current passes through a conductor, a magnetic field is created around the conductor

- In a straight conductor, the induction lines form a system of concentric circles centred on the conductor – see Fig.

- The direction of the lines of force can be found by using the right-hand rule: If the thumb of the right hand points in the direction of the current, the fingers point in the direction of the magnetic field



#### Magnetic induction excited by a long straight wire

- The Biot-Savart law, which gives the relationship for the magnetic induction induced by an electric current, states that the magnitude of the magnetic induction *B* at a point having a distance *a* from the straight conductor through which the current *I* flows is:  $B = \frac{\mu_0 I}{2\pi a}$ 

#### Example 9.2:

Determine the current *I*, which flows through a very long thin straight conductor when the magnitude of the magnetic induction  $B = 5 \cdot 10^{-4}$  T has been found at a distance a = 0.2 m from it. Assume that the conductor is in air ( $\mu_r \cong 1$ ), the permeability of the vakuum  $\mu_0 = 4\pi \cdot 10^{-7}$  H/m. [*I* = 500 A]

#### Force on the moving charge in a magnetic field

- A magnetic force  $\vec{F}_m = Q(\vec{v} \times \vec{B})$  acts on a particle with a charge Qmoving with a velocity  $\vec{v}$  in a magnetic field of induction  $\vec{B}$ 

-  $\vec{F}_m$  – vector product; the magnetic force vector  $\vec{F}_m$  – always perpendicular to the vectors of induction  $\vec{B}$  and velocity  $\vec{v}$ 

- The magnitude of the force:  $F_{\rm m} = Q v B \sin \alpha$ 

 $(\alpha - \text{the angle between vectors } \vec{v} \text{ and } \vec{B})$ 

- If  $\alpha = 0^{\circ}$  or  $\alpha = 180^{\circ}$  ( $\vec{v} \uparrow \uparrow \vec{B}$ ,  $\vec{v} \uparrow \downarrow \vec{B}$ ) – a charged particle moves parallel or antiparallel to the magnetic field  $\Rightarrow$  the magnetic force = 0  $\Rightarrow$ 

 $\Rightarrow$  the particle continues in its uniform straight-line motion ( $\vec{v}$  = const.)

- For the charge moving perpendicular to the magnetic field ( $\alpha = 90^\circ$ ,  $\vec{v} \perp \vec{B}$ )  $\Rightarrow$  The maximum value of the force  $F_m = Q \vee B \sin \alpha = Q \vee B$
- $\vec{F}_m$  also perpendicular to velocity  $\vec{v} \Rightarrow$  so it must be a centripetal force  $\vec{F}_c$ (is directed to the centre of the circle):

$$F_m = F_c \Leftrightarrow QvB = \frac{mv^2}{r}$$

- The trajectory of a charged particle entering the magnetic field perpendicular to the direction of the induction lines is a circle of radius *r* 

#### Example 9.6:

The electron enters a homogeneous magnetic field of induction  $B = 1 \mu T$ perpendicular to the direction of the induction lines - see Fig. - with speed v = 1000 m/s and starts moving in a circle. What is the radius *r* of this circle? The charge of the electron  $e = 1.6 \cdot 10^{-19}$  C, the mass of the electron  $m = 9.1 \cdot 10^{-31}$  kg.

[*r* = 5.7 mm]



#### Application

- <u>Mass spectrometer</u> is used to determine the mass of atoms or molecules
   see Fig.
- Positive ions are produced in the source S
- Only those ions whose velocity is v = E / B will pass through the selector in an electric field of intensity  $\vec{E}$  and a magnetic field of induction  $\vec{B}$
- These ions pass through the divider  $S_v$
- Furthermore, there is only a magnetic field of induction  $\vec{B}$ , which is perpendicular to the ion velocity  $(\vec{B} \perp \vec{v}) \Rightarrow$  the ions move in a circular path
- The ions illuminate the photographic plate at the point where they fall (the radius of the path *r* is measured)
- By measuring from a mark on the photographic plate, the mass of any particle can be accurately determined



- We can determine the mass of ions *m* as function of radius *r* :

$$\frac{mv^2}{r} = QvB \Rightarrow m(r) = \frac{QBr}{v} = \frac{QB^2r}{E}$$

#### Force on the wire conductor in a magnetic field

- A conductor with a constant current placed in a magnetic field  $\Rightarrow$  a force is applied to it

The magnitude of the magnetic force:  $F_m = I \, l \, B \, sin \, \alpha$ ,

where: *I* – magnitude of current flowing through the conductor,

- *l* length of conductor
- **B** magnitude of magnetic induction
- $\alpha$  angle between the conductor and magnetic induction

#### Force between two parallel conductors

- If two conductors through which a current flows are placed side by side, then each of them is in the magnetic field of the conductor and is subject to a force perpendicular both to its own current and to the magnetic field of the other conductor



If the currents are in the same direction, the force is attractive
If the currents are in opposite directions, the force is repulsive – see Fig.

Force magnitude  $F_{1,2}$  per length *l* of conductor:  $F_{1,2} = \frac{\mu_0 I_1 I_2 l}{2\pi a}$ 

#### Application

- This equation is used to define the ampere (A), one of the seven SI base units – if  $I_1 = I_2 = 1$  A, and the wires are 1 m apart ( $\mu_0 = 4\pi \cdot 10^{-7}$  H/m)

<u>One ampere</u> – the current flowing in each two long parallel wires, placed in a vacuum 1 metre apart, which produces a force between them 2.10<sup>-7</sup> newtons per metre length

- <u>Electric motor</u> a machine for converting electrical energy into mechanical energy
- It works on the principle that current passing through a loop in a magnetic field exerts a force that can rotate the loop
- Since the currents in the loop have opposite directions, the directions of the forces induced by the magnetic field are opposite
- One side of the loop moves up and the other down see Fig. The result is torque and rotation of the loop



#### **Electromagnetic induction**

- If we move a conductor in a magnetic field, a current flows through it and an electromotive force is induced at the ends of the conductor
- The electric current in the conductor is also induced by the changing magnetic field
- We speak of electromagnetic induction

**Faraday's law of electromagnetic induction**:  $u = -\frac{d\Phi}{dt}$ 

 The induced e.m.f. (voltage) = the negative change in magnetic flux over time

- The direction of the induced voltage is indicated by the minus sign -Lenz's law: The direction of the induced e.m.f. is such that it acts against the change that induces it

- <u>Magnetic flux</u>:  $\boldsymbol{\Phi} = \vec{B} \cdot \vec{A} = B \cdot A \cos \alpha$ , where
- $\vec{A}$  is the vector perpendicular to the area A through which the magnetic field of induction  $\vec{B}$  passes,
- $\alpha$  the angle between vectors  $\vec{A}$  and  $\vec{B}$  see Fig.
- The magnetic flux  $\Phi$  changes over time if the magnitude of the magnetic induction *B* or the size of the area *A* or the angle  $\alpha$  change
- SI unit of magnetic flux weber:
   [\$\phi\$] = [\$B].[\$A] = T.m<sup>2</sup> = Wb



Magnetic flux

#### **Inductance**

- The changing current flowing through the coil  $\Rightarrow$  the changing magnetic field around the coil  $\Rightarrow$  e.m.f. in this coil
- If a varying current *i*(*t*) passes through the coil, the coil induces a voltage (e.m.f.) at its ends *self inductance L*
- [*L*] = H (henry)

 $\phi \sim i$ ,  $\phi = L i$  (magnetic flux  $\phi$  is proportional to current *i*)

From Faraday's law: 
$$u = -\frac{d\Phi}{dt} = -L\frac{di}{dt}$$

- If two coils are placed close together, the changing current in one coil will cause e.m.f. in the other – *mutual inductance M* 

#### Application

#### **Alternating current**

- The most important practical result of Faraday's discovery – the generation of the alternating current (symbol a.c. or AC)



- An electric generator transforms mechanical energy into electric energy - An alternating-current generator – a loop (coil) of area A that rotates in the uniform magnetic field  $\vec{B}$ produced by permanent magnet – see Fig.

- The frequency *f* of the alternating current (voltage) produced =
- = the frequency f at which the loop rotates (angular velocity  $\omega = 2\pi f$ )
- From Faraday's law of electromagnetic induction:

Induced voltage  $u = -\frac{d\Phi}{dt}$ , where  $\Phi = \overrightarrow{B} \cdot \overrightarrow{A} = B \cdot A \cos \alpha$ 

- We assume: for time t = 0 the angle  $\alpha$  between the vectors  $\vec{B}$  and  $\vec{A} = 0 \Rightarrow \Rightarrow \phi(0) = B A$ 

 $\alpha = \omega t \Rightarrow$  magnetic flux  $\phi(t) = B A \cos \alpha = B A \cos \omega t \Rightarrow$ 

 $\Rightarrow$  the instantaneous value of voltage at time *t*:

$$u = -\frac{d\Phi}{dt} = -\frac{d(BA\cos\omega t)}{dt} = \omega BA\sin\omega t = U_0\sin\omega t$$

- The output voltage u(t) sinusoidal with amplitude  $U_0 = \omega BA$  and angular frequency  $\omega = 2\pi f = \frac{2\pi}{T}$  (*T* is the period)
- The graph of voltage versus time a sinusoidal function see Fig.



#### Example 9.16:

- A flat square coil with side a = 0.12 m has N = 10 turns of very thin wire. The coil rotates uniformly in a homogeneous magnetic field of induction magnitude B = 0.25 T about an axis passing through its centre (parallel to the side of the square) and lying in the plane of the coil perpendicular to the vector  $\vec{B}$  - see Fig. Determine the magnitude of the angular velocity of rotation of the coil  $\omega$ , if the maximum value of the voltage induced in the
- coil is  $U_0 = 20$  V.
- [*ω* = 556 rad/s]



- Unlike direct current (DC), the value of alternating current (and voltage) (AC) varies continuously
- Therefore, we define the effective value of voltage and current

- For a sinusoidal waveform:  $U_{ef} = \frac{U_0}{\sqrt{2}}$  ,  $I_{ef} = \frac{I_0}{\sqrt{2}}$ 



Phase difference between voltage and current

In AC circuits, the voltage and corresponding current are generally not in phase
They are shifted by the phase angle φ – see Fig.

**Electric power** 

The average power  $\overline{P}$  for AC current:

$$\overline{P} = U_{ef} I_{ef} \cos\varphi \qquad (P = UI \text{ for DC current}),$$

where  $U_{ef}$  and  $I_{ef}$  – the effective values of voltage and current,  $\varphi$  – phase angle,

 $\cos \varphi$  – power factor of the circuit