

# Thermodynamics

- **Thermodynamics** deals with the conversion of energy from one form to another and the availability of energy for doing work
- **Internal energy** – the total kinetic energy and potential energy of atoms and molecules of the system
- **Temperature** – a measure of the hotness or coldness of an object
- **Heat** – the process of energy transfer from one body or system to another as a result of a difference in temperature

# Thermodynamics

- **Three methods of heat transfer:**
- **Convection – involves the bulk motion of a fluid and is usually caused by a hot fluid (with less dense) rising and displacing colder fluid**
- **Conduction – the transfer of heat in solids and liquids from a region of higher temperature to a region of lower temperature, primarily by collisions and vibrations between particles**
- **Radiation – includes the emission and absorption of electromagnetic radiation**

# Thermodynamics

- Temperature – the important thermodynamic property

Two objects in thermal contact will be at the same temperature, if there is no flow of heat between these two objects (*thermodynamics equilibrium*)

- If there is a flow of heat energy from one object to the second one, then the object that is the source of heat, must be at a higher temperature than the object that accepts the heat energy
- The Celsius temperature scale uses the freezing point of distilled water (defined as  $0^{\circ}\text{C}$ ) and its boiling point ( $100^{\circ}\text{C}$ ) as the two fixed points and divides the scale between them into 100 degrees (at standard atmospheric pressure)

# Thermodynamics

- The thermodynamic temperature scale (Kelvin scale) is based on the measurement of the amount of heat flowing between bodies at different temperatures
- This scale is based on the temperature at which no body can give off heat (absolute zero 0)
- Relation between these two scales:  $T = 273.15 + t$ ,
- $T$  – temperature in kelvins (K),  $t$  – temperature in Celsius degrees ( $^{\circ}\text{C}$ )
- The value 273.15 – the temperature of the melting point of ice in kelvins
- the temperature difference  $\Delta T = T_2 - T_1$  in kelvins is exactly equal to the temperature difference  $\Delta t = t_2 - t_1$  in Celsius degrees:
- $\Delta T = \Delta t$

# Thermodynamics

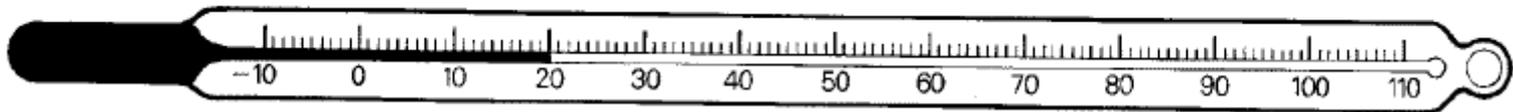
- **Thermal expansion of solids and liquids (expansivity)**
- ***Linear expansion***
- **If the temperature of a metal rod of length  $l_1$  is increasing from  $t_2$  to  $t_1$  ( $\Delta t = t_2 - t_1$ ) its length expands by an amount  $\Delta l = l_1 \alpha \Delta t$**
- **Constant  $\alpha$  – the coefficient of linear expansion of the material**
- **The value of  $\alpha$  depends on the material - unit  $[\alpha] = \text{K}^{-1}$**
- **Different materials expand at different rates when heated**
- **The total length of rod  $l_2$  after increasing temperature:**
- **$l_2 = l_1 + \Delta l = l_1 (1 + \alpha \Delta t)$**

# Thermodynamics

- **Thermal expansion of solids and liquids (expansivity)**
- ***Volume expansion***
- **Analogically to the previous one dimensional case, the volume expansion concerns all three dimensions of solids or liquids**
- **the volume expands with increasing temperature:  $\Delta V = V_1 \beta \Delta t$**
- **$\Delta V$  – increase in volume**
- **$V_1$  – initial volume ( for temperature  $t_1$ )**
- **$\Delta t = t_2 - t_1$  – change of temperature**
- **$\beta = 3\alpha$  – coefficient of volume expansion**
- **The volume of body after change in temperature**
- **$V_2 = V_1 + \Delta V = V_1 (1 + \beta \Delta t)$**

# Thermodynamics

- *Application*
- Temperature measurement
- The basis of a thermometer can be any property that changes with temperature
- A liquid thermometer takes advantage of the fact that the liquid expands as the temperature rises, usually using mercury or alcohol
- These thermometers consist of a glass bulb filled with liquid that is connected to a partially filled capillary tube. As the liquid heats up, it expands and a column of liquid rises up the capillary tube – see Fig.



Mercury thermometer

# Thermodynamics

## Example 7.1:

Calculate at what change in temperature  $\Delta t$  the steel strip  $l_1 = 50$  m long will extend by a length  $\Delta l = 1$  mm. The coefficient of linear expansion of the steel is  $\alpha = 1.2 \cdot 10^{-5} \text{ K}^{-1}$ .

**$[\Delta t = 1.7 \text{ }^\circ\text{C}]$**

# Thermodynamics

## Heat

- Heat – internal energy that can be transferred from one body to another if one body has a higher temperature than the other

- Heat  $Q$  – a form of energy  $\Rightarrow$  it is measured in joules  $[Q] = \text{J}$

If there is a flow of heat from one body to another, then the body that is the source of the heat, must have a higher temperature than the body that is receiving the heat energy

- The temperature of the heat source decreases and the temperature of the object receiving the heat energy increases, heat is transferred until the two temperatures are equal – *thermodynamic equilibrium*

- If an amount of heat  $Q$  is added to a body of mass  $m$ , the temperature rises by  $\Delta t$

# Thermodynamics

$C = \frac{Q}{\Delta t}$  – the *heat capacity of body* – the heat required to produce a unit temperature rise

- SI unit of heat capacity  $[C] = \text{J}\cdot\text{K}^{-1}$

$c = \frac{Q}{m \Delta t}$  – the *specific heat capacity* of a substance – the heat required to produce a unit temperature rise per unit mass of substance

- SI unit of specific heat capacity  $[c] = \text{J}\cdot\text{kg}^{-1}\cdot\text{K}^{-1}$

- If the temperature of a body of mass  $m$  and specific heat capacity  $c$  increases by the temperature difference  $\Delta t$ , a quantity of heat  $Q$  must be supplied:  $Q = c m \Delta t$

# Thermodynamics

## Calorimetric Equation

- If we combine the hot and cold substances (masses  $m_1, m_2$ , specific heat capacities  $c_1, c_2$  and temperatures  $t_2 > t_1$ ), everything settles at the final temperature  $t$  ( $t_2 > t > t_1$ ) – *thermodynamic equilibrium*

- Then, assuming that there is no conversion of heat to other forms of energy, and assuming that there is no heat loss to the surroundings (insulated system), the total energy is conserved - the *Principle of conservation of energy*

- The heat given off by the warmer substance  $Q_2$  is equal to the heat received by the cooler substance  $Q_1$ :

$$Q_1 = Q_2 \Leftrightarrow m_1 c_1 (t - t_1) = m_2 c_2 (t_2 - t)$$

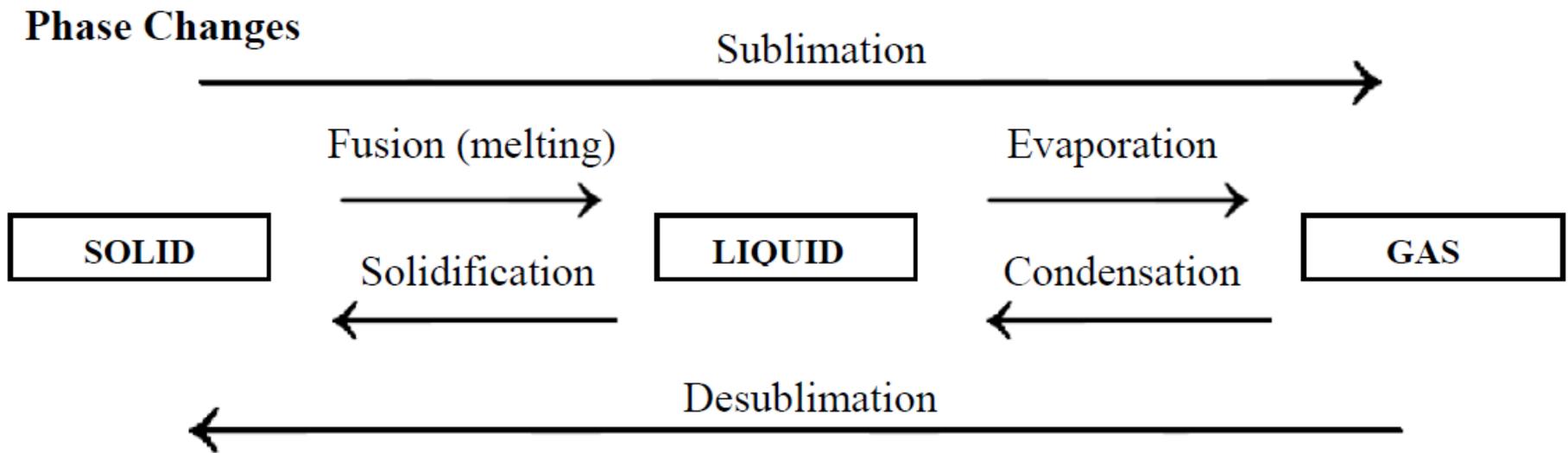
# Thermodynamics

## Example 7.6:

Water with mass  $m_1 = 500$  g and temperature  $t_1 = 17$  °C was in a calorimeter with heat capacity  $C = 25$  J·K<sup>-1</sup>. A metal sample of mass  $m_2 = 200$  g heated to a temperature of  $t_2 = 100$  °C was placed in the water in the calorimeter. The temperature of the water in the calorimeter was then stabilised at  $t = 20$  °C. Determine the specific heat capacity of the metal  $c_2$ . The specific heat capacity of water is  $c_1 = 4200$  J·kg<sup>-1</sup>·K<sup>-1</sup>.

[ $c_2 = 398$  J·kg<sup>-1</sup>·K<sup>-1</sup>]

# Thermodynamics



# Thermodynamics

- When a solid is heated, its temperature rises to the temperature at which the solid begins to melt
- The supplied energy is used to change the solid into a liquid without changing the temperature
- Similarly - when a liquid is heated, its temperature rises until the liquid begins to boil – the change from liquid to gas takes place without a change in temperature
- Latent heat  $Q$ : the amount of heat absorbed by a substance during the change of phase
- $l = \frac{Q}{m}$  – specific latent heat: the heat per unit mass of a substance required (or released) to convert one phase (solid, liquid or gas) to another at a constant temperature
- SI unit of specific latent heat  $[l] = \text{J}\cdot\text{kg}^{-1}$

# Thermodynamics

**Example - Phase changes – ice, water, steam:**

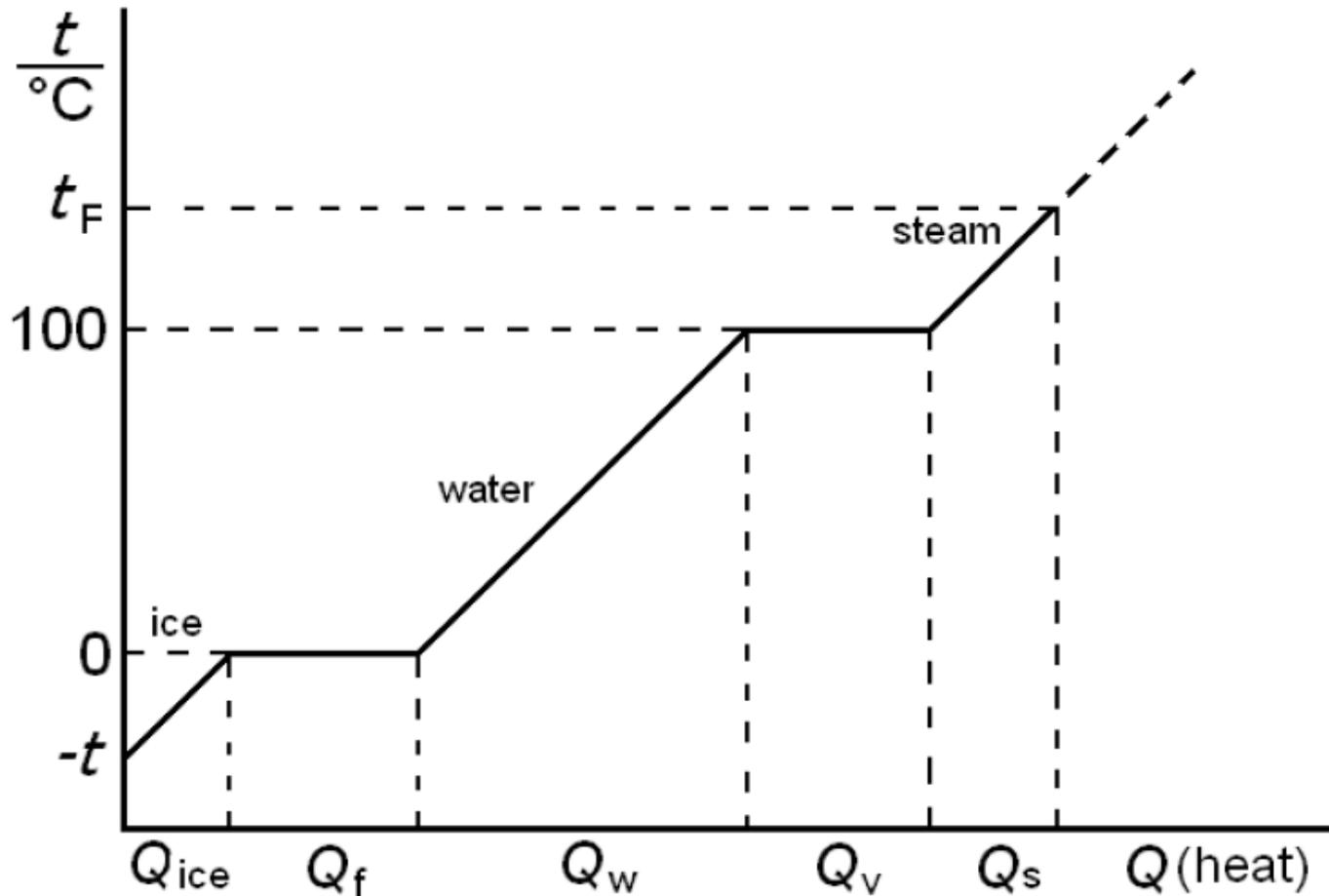


Diagram of phase changes

# Thermodynamics

- When the ice is heated, its temperature rises until it starts to melt (fusion)  $Q_{\text{ice}}$  – the amount of heat required to change the temperature of ice from initial negative temperature  $t$  to  $0\text{ }^{\circ}\text{C}$  (melting point):

$$Q_{\text{ice}} = m_{\text{ice}} \cdot c_{\text{ice}} \cdot (0 - t)$$

$t$  – negative temperature of ice

$m_{\text{ice}}$  – mass of ice

$c_{\text{ice}}$  – specific heat capacity of ice ( $c_{\text{ice}} = 2100\text{ J}\cdot\text{kg}^{-1}\cdot\text{K}^{-1}$ )

- Then the latent heat of fusion  $Q_f$  is required to change the ice at  $0\text{ }^{\circ}\text{C}$  to water at  $0\text{ }^{\circ}\text{C}$ :  $Q_f = m_{\text{ice}} \cdot l_f$

$l_f$  – specific latent heat of fusion of ice ( $l_f = 330\text{ kJ}\cdot\text{kg}^{-1}$ )

# Thermodynamics

- The heat  $Q_w$  is required to change the temperature of the water from 0 °C to 100 °C (boiling point):  $Q_w = m_w \cdot c_w \cdot (100 - 0)$

$m_w$  – mass of water ( $m_w = m_{ice}$ )

$c_w$  – specific heat capacity of water ( $c_w = 4200 \text{ J}\cdot\text{kg}^{-1}\cdot\text{K}^{-1}$ )

- Then the latent heat of vaporization  $Q_v$  is required to change the water at 100 °C to steam at 100 °C:  $Q_v = m_w l_w$

$l_w$  – specific latent heat of vaporization of water ( $l_w = 2200 \text{ kJ}\cdot\text{kg}^{-1}$ )

- The heat  $Q_s$  is required to change the temperature of the steam from 100 °C to final temperature  $t_F$ :  $Q_s = m_s c_s (t_F - 100)$

$m_s$  – mass of steam ( $m_s = m_w$ )

$c_s$  – specific heat capacity of steam ( $c_s = 730 \text{ J}\cdot\text{kg}^{-1}\cdot\text{K}^{-1}$ )

# Thermodynamics

## *Application*

- The large specific heat capacity of water causes a temperate climate - a slow and small change in water and air temperature near large bodies of water (sea)
- It is a difference from continental climate over dry areas

# Thermodynamics

## Gases

- The properties of gases from a macroscopic view are described by physical quantities: pressure  $p$  (Pa), volume  $V$  (m<sup>3</sup>) and temperature  $T$  (K)
- The relation for an ideal gas – ideal gas equation:

$$\frac{pV}{T} = \text{const.}, \text{ or for two states of gas: } \frac{p_1V_1}{T_1} = \frac{p_2V_2}{T_2}$$

- If one quantity is constant, then only two quantities of the same amount of gas can be changed:

1 – at constant temperature ( $T = \text{const.}$ ), *isothermal process*:  $pV = \text{const.}$

2 – at constant pressure ( $p = \text{const.}$ ), *isobaric process*:  $\frac{V}{T} = \text{const.}$

3 – at constant volume ( $V = \text{const.}$ ), *isochoric process*:  $\frac{p}{T} = \text{const.}$

# Thermodynamics

- If the state of gas is under normal conditions,

pressure  $p_n = 101.325 \cdot 10^3$  Pa and temperature  $t_n = 0$  °C  $\Rightarrow T_n = 273.15$  K,

then one mole of any gas occupies volume  $V_{mn} = 22.414 \cdot 10^{-3}$  m<sup>3</sup>:

$$\frac{p_n V_{mn}}{T_n} = R_m = 8.314 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}, R_m - \text{universal gas constant}$$

- The ideal gas equation can be written in the form:

$$p V = n R_m T \quad (n - \text{number of moles})$$

- One mole is the number of atoms in 12 g of carbon  $^{12}_6\text{C}$

- This number is called *Avogadro's number*  $N_A = 6.023 \cdot 10^{23}$  mol<sup>-1</sup>

- All gases contain the same number of molecules or atoms when they occupy the same volume at constant conditions (pressure and temperature)

# Thermodynamics

## *Adiabatic process*

If  $\Delta Q = 0 \Rightarrow Q = \text{const.} \Rightarrow$  system is isolated  $\Rightarrow$  no changes of heat between the system and surroundings – *adiabatic process*:

$$p V^{\kappa} = \text{const.}$$

$\kappa = \frac{c_{mp}}{c_{mV}}$  – Poisson's constant of gas – ratio of the molar heat capacities of a gas at constant pressure  $c_{mp}$  and at constant volume  $c_{mV}$

# Thermodynamics

## Example 7.10:

The compressor compressed air of volume  $V_1 = 100$  l, temperature  $t = 10$  °C and pressure  $p_1 = 10^5$  Pa to pressure  $p_2 = 5 \cdot 10^5$  Pa. The air was cooled so that its temperature did not change. What volume  $V_2$  did the air occupy after compression?

[  $V_2 = 20$  l ]